

Data Representation

Tuesday, 3 October 2023 8:47 AM

Number Systems

1. Decimal number system (also called Denary) | base-10 | digits from 0 > 9
2. Binary number system | base-2 | digits 0 & 1
3. Octal number system | base-8 | digits from 0 > 7
4. Hexadecimal number system | base-16 | digits from 0 > 9 & then A > F. 16 digits in total! :3

↳ To convert from Decimal → Hexadecimal

$$\begin{array}{r} 16 \overline{) 138} \\ \underline{8} \\ 138 \end{array} \quad \begin{array}{l} \text{remainder} \\ \downarrow \\ -10 \text{ or } A \end{array} \quad (138)_{10} \rightarrow (8A)_{16}$$

$$\begin{array}{r} 16 \overline{) 278} \\ \underline{16} \\ 118 \end{array} \quad \begin{array}{l} -6 \\ \\ -1 \end{array} \quad (278)_{10} \rightarrow (116)_{16}$$

$$\begin{array}{r} 16 \overline{) 78} \\ \underline{4} \\ 78 \end{array} \quad \begin{array}{l} -14 \text{ or } E \\ \end{array} \quad (78)_{10} \rightarrow (4E)_{16}$$

↳ To convert from hexadecimal → decimal

$$(AB)_{16} \rightarrow (171)_{10}$$

$$\begin{array}{r} \overset{A}{10} \times 16^1 + \overset{B}{11} \times 16^0 \\ 160 + 11 \\ = 171 \end{array}$$

To convert from binary → hexadecimal

$$\text{group it into } (0001, 0110, 0110, 1011)_2 \rightarrow (166B)_{16}$$

sets of 4, starting from the right & if needed, adding extra 0s to the left.

using your knowledge of all the binary → decimal digits (until decimal 15) for each set of 4!
using your knowledge of all the decimal → hexadecimal digits (hexadecimal F, binary 1111) for each.

(15)
A 4 digit set in binary would be what gives you the last single hexadecimal digit!
(15)

↑ opposite process :3

To convert from hexadecimal → binary

$$(206F)_{16} \rightarrow (0010\ 1101\ 0110\ 1111)_2$$

$$\begin{array}{cccc} 2 & D & 6 & F \\ 2 & 13 & 6 & 15 \\ 0010 & , & 1101 & , & 0110 & , & 1111 \end{array}$$

make sure to add extra 0s if needed, to make each set have 4 digits

To add 2 binary numbers directly ~

$$1101 + 11$$

$$\begin{array}{r} 1\ 1\ 1\ 0\ 1 \\ + \\ \hline 1\ 0\ 0\ 0\ 0 \end{array} \quad \begin{array}{l} \text{is } 2 \text{ or } 10 \end{array}$$

Hexadecimal base-16	Decimal base-10	Binary base-2
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

How numbers are stored in a computer:

Binary numbers are stored in 8 bit+

10 in binary is 1010

it's stored as 00001010 (8 bits!)

*Here, only 7 bits can be used to store the number itself, leftmost bit is reserved for + or - .
2⁷ numbers can be represented, 0 → 127 that's 01111111
128*

-10 in binary is stored as

10001010

The left most digit represents + or -

ASCII - Representation of text in computers:

ASCII, or American Standard Code for Information Interchange, is a character encoding standard for electronic communication.

It is a **7-bit character encoding**, meaning that each character is represented by a unique 7-bit sequence. This allows ASCII to represent a total of 128 different characters.

0 to 9: 48 to 57

A to Z: 65 to 90

a to z: 97 to 122

UNICODE:

It's an established standard for data representation - a single encoding scheme for all languages and characters. The UNICODE data can be used throughout different systems, platforms, and devices (great compatibility).

The difference between UNICODE, and ASCII:

1. Bits used to encode: 32 (UTF 32), 7.
2. Characters representable: over 1 million, 128

The different encoding standards of Unicode are:

UTF-8, UTF-16, UTF-32 (Unicode Transformation Format!)

Pixel Colour Representation

R **G** **B**
| | |
| | |

each R, G, & B value of a pixel is represented from 0 → 255

each is stored in an 8 bit value, so 2⁸ or 256 possible values.

2 hexadecimal digits can represent

256 × 256 × 256 total possible colours a pixel can (generally) display.